

Effect of Aluminum Content on Lattice Parameters and Unit Cell Volume in Bulk Crystals β -(Al_xGa_{1-x})₂O₃

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Abstract

The article studies the influence of aluminum on the lattice parameters and the unit cell volume of the binary solid solution β -(Al_xGa_{1-x})₂O₃. The aluminum content is determined by energy-dispersive X-ray spectroscopy. The lattice parameter values are calculated using X-ray diffractometry data. The diffraction patterns show peak broadening and shift to higher angles with increasing aluminum content. It is shown that when the aluminum fraction x changes from 0 to 0.25, the lattice parameters decrease linearly. This is consistent with Vegard's law for solid solutions. The decrease in cell volume is physically related to the fact that aluminum has a smaller ionic radius than gallium, and the Al–O bond length is shorter than Ga–O one.

Keywords: Aluminum gallium oxide; Bulk crystal; Unit cell; Lattice parameters

1. INTRODUCTION

Gallium oxide β -Ga₂O₃ is a fairly well-studied material at present in terms of both its crystal structure and electronic properties. Gallium oxide research has now shifted to the field of device applications [1]. At the same time, its binary solid solutions with other metal oxides, such as β -(Al_xGa_{1-x})₂O₃ or β -(In_xGa_{1-x})₂O₃, have been studied to a somewhat lesser extent. However, such ternary compounds allow increasing or decreasing the band gap of the material, which is the basis for engineering device heterostructures based on gallium oxide. Therefore, the effect of a substitution impurity, such as aluminum in β -(Al_xGa_{1-x})₂O₃, on the properties of the material (primarily on the crystal lattice) is of considerable interest.

In order to study the influence of aluminum on the properties of the lattice in the compound β -(Al_xGa_{1-x})₂O₃, it is necessary to determine, firstly, the preferred position

that aluminum occupies in the crystal lattice, and, secondly, the lattice parameters of the oxides that make up the ternary compound, namely: Ga₂O₃ and Al₂O₃.

The monoclinic crystal structure of β -Ga₂O₃ has two nonequivalent cationic sites for the gallium ion: the tetrahedrally coordinated site (Ga1) and the octahedrally coordinated site (Ga2). Fig. 1 shows a cell of the monoclinic lattice of β -Ga₂O₃. The tetrahedral and octahedral sites of the gallium ions are shown in blue and green, respectively. The O1, O2 and O3 represent three different sites of the oxygen ions in the β -Ga₂O₃ crystal lattice.

Calculations [2,3] show that it is energetically more favorable for Al to occupy the Ga2 sites. Aluminum located in the octahedral Ga2 sites has an energy of 0.2 eV per Al atom lower than aluminum located in the tetrahedral Ga2 sites [4]. Aluminum atoms begin to occupy the Ga2 sites at sufficiently large values x of the aluminum content in the crystal. According to the data of work [5], during the

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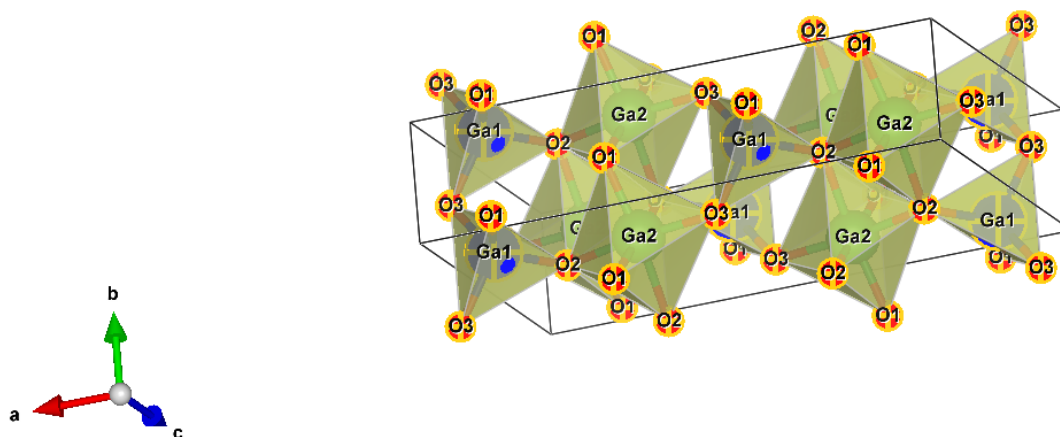


Fig. 1. Unit cell of the β -Ga₂O₃ crystal structure.

growth of bulk β -(Al_xGa_{1-x})₂O₃ crystals, aluminum begins to occupy the Ga1 sites at $x > 0.50$. In our case, for $x < 0.25$, we can assume that aluminum replaces gallium in the octahedral sites only.

According to the literature, the lattice parameter values of gallium oxide β -Ga₂O₃ differ among most researchers starting from the second decimal place [6]. For our studies, the lattice parameters of binary compounds were taken from database cards ICDD PDF-2 release 2014 [7]:

- β -Ga₂O₃ C2/m — 00-041-1103;
- θ -Al₂O₃ C2/m — 01-079-1559.

Note that, strictly speaking, the theta phase of aluminum oxide θ -Al₂O₃, which has the same monoclinic crystal lattice structure as β -Ga₂O₃, is stable only at temperatures below 800 °C [8]. At crystal growth temperatures of 1850 °C, only the alpha phase of aluminum oxide α -Al₂O₃ can stably exist as a substantive material. However, since during the synthesis of the binary solid solution β -(Al_xGa_{1-x})₂O₃, aluminum is incorporated into the sites of the monoclinic lattice of β -Ga₂O₃, the parameters of θ -Al₂O₃, which has a similar structure, are used for comparison.

2. EXPERIMENTS

In this work three samples were studied: pure gallium oxide β -Ga₂O₃ ($x = 0$), β -(Al_{0.11}Ga_{0.89})₂O₃ ($x = 0.11$, 4.4 at.% of Al in crystal) and β -(Al_{0.25}Ga_{0.75})₂O₃ ($x = 0.25$, 10 at.% of Al in crystal). The processes of growing bulk crystals of β -Ga₂O₃ and β -(Al_xGa_{1-x})₂O₃ were carried out in the facility “Nika-3” (production of EZAN, Russia), designed for crystal growth from the melt by the Czochralski method. The procedure for growing bulk crystals is described in more detail in Refs. [9,10].

To analyze the influence of aluminum on the lattice parameters and the unit cell volume of β -(Al_xGa_{1-x})₂O₃, the X-ray diffraction curves (shown in Fig. 2) were obtained from powders ground in an agate mortar on a D2Phaser powder

X-ray diffractometer (Bruker AXS, Germany). Diffractometer equipped with a copper X-ray tube with a nickel β -filter (CuK _{α 1,2}-radiation), a LYNXEYE semiconductor linear position-sensitive X-ray detector (Bruker AXS, Germany) with an opening of 5 angular degrees, and a vertical θ - θ goniometer with Bragg–Brentano focusing. The curves were recorded in the range of angles of 10–120 angular degrees on the 2θ scale, the registration step was 0.02 degrees, the exposure time at a point was 15 seconds.

The phase composition of the powders was determined using the specialized EVA software package (Bruker AXS, Germany) based on the ICDD PDF-2 diffraction database, release 2014 [7]. The calculation of the unit cell parameters of β -Ga₂O₃ and the determination of the features of the crystal structure of the samples were carried out by the Rietveld method with the Topas 5 software package (Bruker AXS, Germany). To eliminate random errors in determining the position of diffraction maxima, an internal NaCl standard verified with Si640f powder silicon (NIST, Gaithersburg, MD, USA) was used.

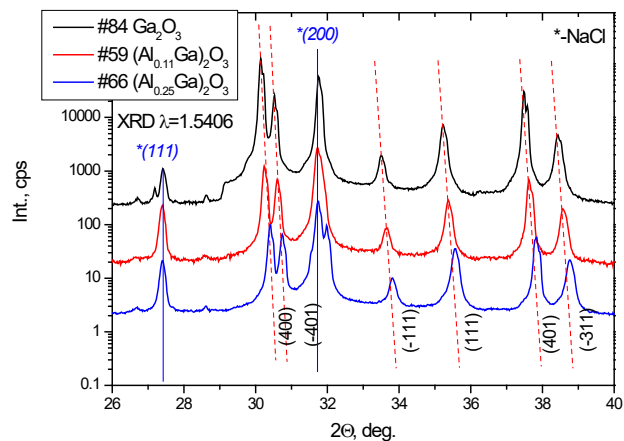
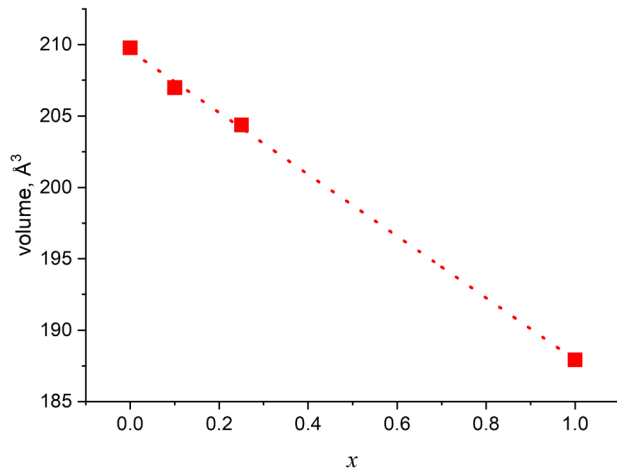
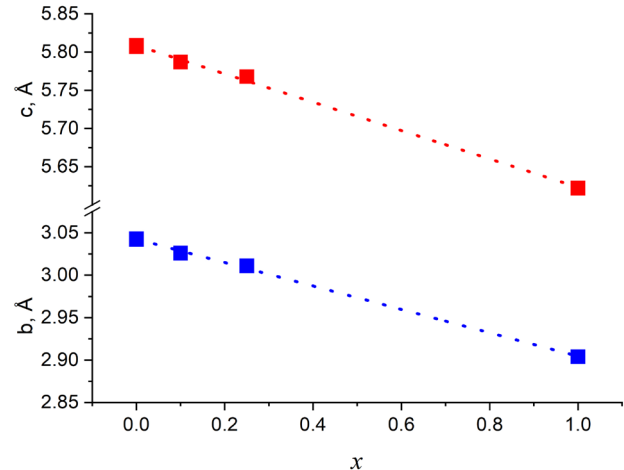
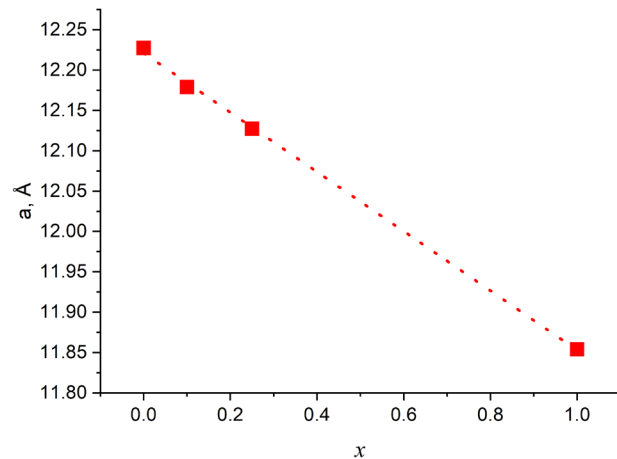


Fig. 2. 2θ -scans X-ray diffraction of β -(Al_xGa_{1-x})₂O₃ samples with different aluminum content x .

Table 1. Calculation data for lattice parameters and unit cell volume.

Sample	a , Å	b , Å	c , Å	Volume, Å ³	Al content, at.% (EDS)	Al content, x (EDS)
β -Ga ₂ O ₃ (C2/m – 00-041-1103)	12.227	3.039	5.808	209.55	0	0
84, β -Ga ₂ O ₃	12.232	3.042	5.809	209.90	0	0
59, β -(Al _{0.11} Ga _{0.89}) ₂ O ₃	12.179	3.026	5.787	206.99	4.4	0.11
66, β -(Al _{0.25} Ga _{0.75}) ₂ O ₃	12.128	3.011	5.768	204.37	10.0	0.25
θ -Al ₂ O ₃ (C2/m – 01-079-1559)	11.854	2.904	5.622	187.92	40.0	1.00

**Fig. 3.** Dependence of the unit cell volume on the aluminum content x in the β -(Al _{x} Ga_{1- x})₂O₃ crystal. For reference, a tabular value of the unit cell volume for aluminum oxide ($x = 1$) has been added to the graph.**Fig. 5.** Dependence of the lattice constants b (blue symbols) and c (red symbols) on the aluminum content x in the crystal β -(Al _{x} Ga_{1- x})₂O₃.**Fig. 4.** Dependence of the lattice constant a on the content x of aluminum in the crystal β -(Al _{x} Ga_{1- x})₂O₃.

The aluminum content in the samples was measured by energy-dispersive X-ray spectroscopy (EDS) on a Tescan MIRA-3 scanning electron microscope with an Ultim Max attachment for EDS. To check the homogeneity of the aluminum distribution over the volume of the crystal, the aluminum content was measured at five points over the surface area of each sample and then averaged. The deviation from the average value did not exceed 5% in all cases.

3. RESULTS AND DISCUSSION

From Fig. 2 it can be seen that with an increase in the aluminum content, the diffraction peaks shift toward larger angles θ , which indicates a decrease in the lattice parameters, and the width of the peaks increases slightly with an increase of Al, which indicates some deterioration in the crystalline quality of the material.

The obtained values of the lattice parameters (a , b , c) and the volume of the unit cell are given in Table 1. For reference, the tabular values of the parameters for β -Ga₂O₃ and for θ -Al₂O₃ are also given here. For clarity, the dependences of all obtained values on the aluminum content are shown graphically in Figs. 3–5. It is well seen that the lattice parameters decrease with an increase in the aluminum content according to a linear law, which is consistent with Vegard's rule.

The results of determining the average size of coherent scattering regions (CSR) and the magnitude of microstresses obtained from the profile analysis data are presented in Table 2. Here R_{wp} is the profile-weighted divergence factor of the experimental and calculated X-ray diffraction patterns. Analysis of the obtained structural data shows that the broadening of the diffraction peaks with increasing of aluminum content is associated with an increase in microstresses in the structure.

Table 2. Calculation results of microstresses.

Sample	CSR, nm	ϵ_0	R_{wp}
84, β -Ga ₂ O ₃	400	$0.8 \cdot 10^{-4}$	10.5
59, β -(Al _{0.11} Ga _{0.89}) ₂ O ₃	400	$2.1 \cdot 10^{-4}$	10.8
66, β -(Al _{0.25} Ga _{0.75}) ₂ O ₃	400	$3.0 \cdot 10^{-4}$	10.4

The physical interpretation of such behavior of the material is quite clear. The ionic radii of Ga in the tetrahedral and octahedral sites are 61 and 76 pm, respectively, while for Al they are 53 and 67.5 pm, respectively, for the same sites [11]. It is obvious that the substitutional Al ion has smaller ionic radii than the Ga ion for both positions. As a result, the lattice is compressed, which is reflected in the diffraction pattern. Also, the first-principles calculation [12] shows that in β -(Al_xGa_{1-x})₂O₃, the average bond length for the Al–O bonds is shorter than that of the corresponding Ga–O bonds by 3.5%.

There is another significant factor that can influence the decrease in lattice parameters. As is known, bulk gallium oxide crystals growing from a melt always contain oxygen vacancies due to the limitations of the oxygen content in the atmosphere of the growth zone. Based on the calculation of the formation energy from first principles, X. Ma et al. [12] showed that in the presence of an oxygen vacancy at the site adjacent to the Al atom, the average length of the Al–O bond decreases by 1.81% compared to the length of the Ga–O bond in the same position. This leads to additional shrinkage of the lattice volume.

4. CONCLUSION

The introduction of aluminum (substitutional impurity) into bulk crystals of gallium oxide β -Ga₂O₃ and the formation of a binary solid solution β -(Al_xGa_{1-x})₂O₃ leads to a decrease in the lattice parameters and the volume of the unit cell linearly with respect to the fraction x of aluminum in the crystal composition, at least for x values in the range from 0 to 0.25 (from 0 to 10 at.%). This is consistent with Vegard's law for solid solutions.

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REFERENCES

- [1] A.A. Petrenko, Ya.N. Kovach, D.A. Bauman, M.A. Odnoblyudov, V.E. Bougrov, A.E. Romanov, Current State of Ga₂O₃-Based Electronic and Optoelectronic Devices. Brief Review, *Rev. Adv. Mater. Technol.*, 2021, vol. 3, no. 2, pp. 1–26.
- [2] H. Peelaers, J.B. Varley, J.S. Speck, C.G. Van de Walle, Structural and electronic properties of Ga₂O₃-Al₂O₃ alloys, *Appl. Phys. Lett.*, 2018, vol. 112, no. 24, art. no. 242101.
- [3] J.M. Johnson, H.-L. Huang, M. Wang, S. Mu, J.B. Varley, A.F.M. Anhar Uddin Bhuiyan, Z. Feng, N.K. Kalariyal, S. Rajan, H. Zhao, C.G. Van de Walle, J. Hwang, Atomic scale investigation of aluminum incorporation, defects, and phase stability in β -(Al_xGa_{1-x})₂O₃ films, *APL Mater.*, 2021, vol. 9, no. 5, art. no. 051103.
- [4] T.S. Wang, W. Li, C.Y. Ni, A. Janotti, Band gap and band offset of Ga₂O₃ and (Al_xGa_{1-x})₂O₃ alloys, *Phys. Rev. Appl.*, 2018, vol. 10, art. no. 011003.
- [5] B.W. Krueger, C.S. Dandeneau, E.M. Nelson, S.T. Dunham, F.S. Ohuchi, M.A. Olmstead, Variation of band gap and lattice parameters of β -(Al_xGa_{1-x})₂O₃ powder produced by solution combustion synthesis, *J. Am. Ceram. Soc.*, 2016, vol. 99, no. 7, pp. 2467–2473.
- [6] J.A. Spencer, A.L. Mock, A.G. Jacobs, M. Schubert, Y. Zhang, M.J. Tadjer, A review of band structure and material properties of transparent conducting and semiconducting oxides: Ga₂O₃, Al₂O₃, In₂O₃, ZnO, SnO₂, CdO, NiO, CuO, and Sc₂O₃, *Appl. Phys. Rev.*, 2022, vol. 9, no. 1, art. no. 011315.
- [7] *International Centre for Diffraction Data*, Electronic resource, URL: www.icdd.org (accessed: 02.12.2024).
- [8] I. Levin, D. Brandon, Metastable alumina polymorphs: crystal structures and transition sequences, *J. Am. Ceram. Soc.*, 1998, vol. 81, no. 8, pp. 1995–2012.
- [9] D.A. Bauman, D.Iu. Panov, D.A. Zakgeim, V.A. Spiridonov, A.V. Kremleva, A.A. Petrenko, P.N. Brunkov, N.D. Prasolov, A.V. Nashchekin, A.M. Smirnov, M.A. Odnoblyudov, V.E. Bougrov, A.E. Romanov, High-Quality Bulk β -Ga₂O₃ and β -(Al_xGa_{1-x})₂O₃ Crystals: Growth and Properties, *Phys. Status Solidi A*, 2021, no. 20, art. no. 2100335.
- [10] D.A. Zakgeim, D.A. Bauman, D.I. Panov, V.A. Spiridonov, A.V. Kremleva, V.M. Smirnov, M.A. Odnoblyudov, A.E. Romanov, V.E. Bougrov, Growing of bulk β -(Al_xGa_{1-x})₂O₃ crystals from the melt by Czochralski method and investigation of their structural and optical properties, *Appl. Phys. Express*, 2022, vol. 15, art. no. 025501.
- [11] I. Bhaumik, M. Soharab, R. Bhatt, A. Saxena, S. Sah, A.K. Karnal, Influence of Al content on the optical band-gap enhancement and lattice structure of (Ga_{1-x}Al_x)₂O₃ single crystal, *Opt. Mater.*, 2020, vol. 109, art. no. 110351.
- [12] X. Ma, Y. Zhang, L. Dong, R. Jia, First-principles calculations of electronic and optical properties of aluminum-doped β -Ga₂O₃ with intrinsic defects, *Results Phys.*, 2017, vol. 7, pp. 1582–1589.

УДК 548.5

Влияние содержания алюминия на параметры решётки и объём элементарной ячейки в объёмных кристаллах β -(Al_xGa_{1-x})₂O₃

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Аннотация. В статье исследовано влияние алюминия на параметры решётки и объём элементарной ячейки двойного твёрдого раствора β -(Al_xGa_{1-x})₂O₃. Содержание алюминия определено методом энергодисперсионной рентгеновской спектроскопии. Расчёт значений параметров решётки выполнен по данным рентгеновской дифрактометрии. Дифрактограммы демонстрируют уширение пиков и смещение в сторону больших углов при увеличении содержания алюминия. В работе показано, что при изменении доли x алюминия от 0 до 0.25 значения параметров решётки и объёма ячейки линейно убывают. Это согласуется с законом Вегарда для твёрдых растворов. Уменьшение объёма ячейки и параметров решётки физически связывается с тем, что алюминий имеет меньший ионный радиус, чем галлий, а длина связи Al–O меньше, чем длина связи Ga–O.

Ключевые слова: оксид галлия алюминия; объёмные кристаллы; элементарная ячейка; параметры решётки